



## FINAL EXAMINATION

**MARCH 2022(Set 2)**

COURSE TITLE	BUSINESS STATISTICS STATISTICS FOR SOCIAL SCIENCE
COURSE CODE	BMAT3213/RMAT321/ BMAT2213/RMAT2233
DATE/DAY TIME/DURATION	

### INSTRUCTIONS TO CANDIDATES:

1. Please read the instruction under each section carefully.
2. Candidates are reminded not to bring into examination hall/room any form of written materials or electronic gadget except for stationery that is permitted by the Invigilator.
3. Students who are caught breaching the Examination Rules and Regulation will be charged with an academic dishonesty and if found guilty of the offence, the maximum penalty is expulsion from the University.

(This Question Paper consists of **6** Printed Pages including front page)

**\*\*\*DO NOT OPEN THE QUESTION PAPER UNTIL YOU ARE TOLD TO DO SO\*\*\***

**There are 7 questions in this section. Answer all of them**

**(80 marks)**

1. A set of data consists of the following numbers

1 2 2 3 3 3 4 4 4 4 5 5 5 5 5

- a. Find the median and the standard deviation

(8 marks)

- b. Calculate the Pearson's coefficient of skewness

(4 marks)

(12 marks)

2. A bag contains 3 apples, 4 oranges and 5 pears. Six fruits are taken out at random from the bag without replacement. Calculate the probability that

- a. at least one fruit is a pear

(5 marks)

- b. exactly four are oranges given that at least one fruit is a pear

(7 marks)

(12 marks)

3. The number of trees planted at FRIM is not more than four trees in a day.

The probability that there is no tree planted in a day is 0.4 and the probabilities that there are at most one, two and three trees planted in a day are 0.7, 0.85 and 0.95 respectively.

- a. Construct a probability distribution table for the number of trees planted.

(6 marks)

- b. Calculate the mean of the number of trees planted in a day.

(6 marks)

(12 marks)

4. The masses of guavas in a farm are normally distributed with a mean  $\mu$  and a standard deviation,  $\sigma$ . The mass of percentages of guava that less than 400 g is 15.87% and more than 500 g is 6.68%.

Determine the values of  $\mu$  and  $\sigma$

(10 marks)

5. A fruit stall sells tomatoes, apricots and plums. The weights of plums are normally distributed with a mean of 80 grams and standard deviation 4 grams. Five plums are chosen at random, find the probability exactly three of them weigh more than 82 grams.

(10 marks)

6. The heights of a new species of plants have a mean of 2 m and a standard deviation of 40 cm. 100 samples of 50 plants each are measured. Find the number of samples expected when the sample mean is

a. greater than 2.10 m

(5 marks)

b. between 1.95 m and 2.05 m

(7 marks)

(12 marks)

7. In each of the following cases, given the population standard deviation  $\sigma$ , the statement claim about  $\mu$ , the sample size  $n$ , and the level of significance  $\alpha$ , find

- a. the null and alternate hypotheses  
b. the test statistics  
c. the rejection regions

i.  $\sigma = 2.5$  claim:  $\mu > 35$ ,  $n = 65$ ,  $\alpha = 0.01$

(6 marks)

ii.  $\sigma = 0.6$  claim:  $\mu \neq 3.2$ ,  $n = 50$ ,  $\alpha = 0.05$

(6 marks)

(12 marks)

SULIT

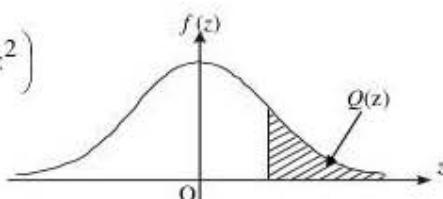
## THE UPPER TAIL PROBABILITY $Q(z)$ FOR THE NORMAL DISTRIBUTION $N(0,1)$

### KEBARANGKALIAN HUJUNG ATAS $Q(z)$ BAGI TABURAN NORMAL $N(0, 1)$

z	0	1	2	3	4	5	6	7	8	9	1	2	3	4	5	6	7	8	9
		Mimas / Tolak																	
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641	4	8	12	16	20	24	28	32	36
0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247	4	8	12	16	20	24	28	32	36
0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859	4	8	12	15	19	22	26	30	34
0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483	4	7	11	15	19	22	26	30	34
0.4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121	4	7	11	15	18	22	25	29	32
0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776	3	7	10	14	17	20	24	27	31
0.6	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2483	0.2451	3	7	10	13	16	19	23	26	29
0.7	0.2420	0.2389	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148	3	6	9	12	15	18	21	24	27
0.8	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867	3	5	8	11	14	16	19	22	25
0.9	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611	3	5	8	10	13	15	18	20	23
1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379	2	5	7	9	12	14	16	19	21
1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170	2	4	6	8	10	12	14	16	18
1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985	2	4	6	7	9	11	13	15	17
1.3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823	2	3	5	6	8	10	11	13	14
1.4	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681	1	3	4	6	7	8	10	11	13
1.5	0.0668	0.0655	0.0643	0.0630	0.0618	0.0606	0.0594	0.0582	0.0571	0.0559	1	2	4	5	6	7	8	10	11
1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455	1	2	3	4	5	6	7	8	9
1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367	1	2	3	4	4	5	6	7	8
1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294	1	1	2	3	4	4	5	6	6
1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233	1	1	2	2	3	4	4	5	5
2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183	0	1	1	2	2	3	3	4	4
2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143	0	1	1	2	2	2	3	3	4
2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110	0	1	1	1	2	2	2	3	3
2.3	0.0107	0.0104	0.0102		0.00990	0.00964	0.00939	0.00914			0	1	1	1	1	2	2	2	2
											3	5	8	10	13	15	18	20	23
2.4	0.00820	0.00798	0.00776	0.00755	0.00734		0.00714	0.00695	0.00676	0.00657	0.00639	2	5	7	9	12	14	16	19
2.5	0.00621	0.00604	0.00587	0.00570	0.00554	0.00539	0.00523	0.00508	0.00494	0.00480	2	3	5	6	8	9	11	13	17
2.6	0.00466	0.00453	0.00440	0.00427	0.00415	0.00402	0.00391	0.00379	0.00368	0.00357	1	2	3	5	6	7	9	9	10
2.7	0.00347	0.00336	0.00326	0.00317	0.00307	0.00298	0.00289	0.00280	0.00272	0.00264	1	2	3	4	5	6	7	8	9
2.8	0.00256	0.00248	0.00240	0.00233	0.00226	0.00219	0.00212	0.00205	0.00199	0.00193	1	1	2	3	4	4	5	6	6
2.9	0.00187	0.00181	0.00175	0.00169	0.00164	0.00159	0.00154	0.00149	0.00144	0.00139	0	1	1	2	2	3	3	4	4
3.0	0.00135	0.00131	0.00126	0.00122	0.00118	0.00114	0.00111	0.00107	0.00104	0.00100	0	1	1	2	2	3	3	4	4

$$f(z) = \frac{1}{\sqrt{2\pi}} \exp\left(-\frac{1}{2}z^2\right)$$

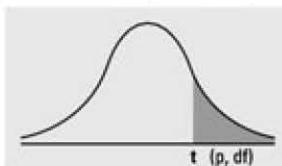
$$Q(z) = \int_k^{\infty} f(z) dz$$



#### **Example / Contoh:**

If  $X \sim N(0, 1)$ , then  $P(X > k) = Q(k)$

Numbers in each row of the table are values on a  $t$ -distribution with ( $df$ ) degrees of freedom for selected right-tail (greater-than) probabilities ( $p$ ).



<b>df/p</b>	<b>0.40</b>	<b>0.25</b>	<b>0.10</b>	<b>0.05</b>	<b>0.025</b>	<b>0.01</b>	<b>0.005</b>	<b>0.0005</b>
<b>1</b>	0.324920	1.000000	3.077684	6.313752	12.70620	31.82052	63.65674	636.6192
<b>2</b>	0.288675	0.816497	1.885618	2.919986	4.30265	6.96456	9.92484	31.5991
<b>3</b>	0.276671	0.764892	1.637744	2.353363	3.18245	4.54070	5.84091	12.9240
<b>4</b>	0.270722	0.740697	1.533206	2.131847	2.77645	3.74695	4.60409	8.6103
<b>5</b>	0.267181	0.726687	1.475884	2.015048	2.57058	3.36493	4.03214	6.8688
<b>6</b>	0.264835	0.717558	1.439756	1.943180	2.44691	3.14267	3.70743	5.9588
<b>7</b>	0.263167	0.711142	1.414924	1.894579	2.36462	2.99795	3.49948	5.4079
<b>8</b>	0.261921	0.706387	1.396815	1.859548	2.30600	2.89646	3.35539	5.0413
<b>9</b>	0.260955	0.702722	1.383029	1.833113	2.26216	2.82144	3.24984	4.7809
<b>10</b>	0.260185	0.699812	1.372184	1.812461	2.22814	2.76377	3.16927	4.5869
<b>11</b>	0.259556	0.697445	1.363430	1.795885	2.20099	2.71808	3.10581	4.4370
<b>12</b>	0.259033	0.695483	1.356217	1.782288	2.17881	2.68100	3.05454	4.3178
<b>13</b>	0.258591	0.693829	1.350171	1.770933	2.16037	2.65031	3.01228	4.2208
<b>14</b>	0.258213	0.692417	1.345030	1.761310	2.14479	2.62449	2.97684	4.1405
<b>15</b>	0.257885	0.691197	1.340606	1.753050	2.13145	2.60248	2.94671	4.0728
<b>16</b>	0.257599	0.690132	1.336757	1.745884	2.11991	2.58349	2.92078	4.0150
<b>17</b>	0.257347	0.689195	1.333379	1.739607	2.10982	2.56693	2.89823	3.9651
<b>18</b>	0.257123	0.688364	1.330391	1.734064	2.10092	2.55238	2.87844	3.9216
<b>19</b>	0.256923	0.687621	1.327728	1.729133	2.09302	2.53948	2.86093	3.8834
<b>20</b>	0.256743	0.686954	1.325341	1.724718	2.08596	2.52798	2.84534	3.8495
<b>21</b>	0.256580	0.686352	1.323188	1.720743	2.07961	2.51765	2.83136	3.8193
<b>22</b>	0.256432	0.685805	1.321237	1.717144	2.07387	2.50832	2.81876	3.7921
<b>23</b>	0.256297	0.685306	1.319460	1.713872	2.06866	2.49987	2.80734	3.7676
<b>24</b>	0.256173	0.684850	1.317836	1.710882	2.06390	2.49216	2.79694	3.7454
<b>25</b>	0.256060	0.684430	1.316345	1.708141	2.05954	2.48511	2.78744	3.7251
<b>26</b>	0.255955	0.684043	1.314972	1.705618	2.05553	2.47863	2.77871	3.7066
<b>27</b>	0.255858	0.683685	1.313703	1.703288	2.05183	2.47266	2.77068	3.6896
<b>28</b>	0.255768	0.683353	1.312527	1.701131	2.04841	2.46714	2.76326	3.6739
<b>29</b>	0.255684	0.683044	1.311434	1.699127	2.04523	2.46202	2.75639	3.6594
<b>30</b>	0.255605	0.682756	1.310415	1.697261	2.04227	2.45726	2.75000	3.6460
<b>z</b>	0.253347	0.674490	1.281552	1.644854	1.95996	2.32635	2.57583	3.2905
<b>CI</b>	—	—	80%	90%	95%	98%	99%	99.9%

		Table A.7 Critical Values of the F Distribution for $\alpha = .05$																		
		df NUMERATOR																		
df Denominator	1	2	3	4	5	6	7	8	9	10	12	15	20	25	30	40	60	120	$\infty$	
3	10.13	9.55	9.28	9.12	9.01	8.94	8.89	8.85	8.81	8.79	8.74	8.70	8.66	8.63	8.62	8.59	8.57	8.55	8.53	
4	7.71	6.94	6.59	6.39	6.26	6.16	6.09	6.04	6.00	5.96	5.91	5.86	5.80	5.77	5.75	5.72	5.69	5.66	5.63	
5	6.61	5.79	5.41	5.19	5.05	4.95	4.88	4.82	4.77	4.74	4.68	4.62	4.56	4.52	4.50	4.46	4.43	4.40	4.36	
6	5.99	5.14	4.76	4.53	4.39	4.28	4.21	4.15	4.10	4.06	4.00	3.94	3.87	3.83	3.81	3.77	3.74	3.70	3.67	
7	5.59	4.74	4.35	4.12	3.97	3.87	3.79	3.73	3.68	3.64	3.57	3.51	3.44	3.40	3.38	3.34	3.30	3.27	3.23	
8	5.32	4.46	4.07	3.84	3.69	3.58	3.50	3.44	3.39	3.35	3.28	3.22	3.15	3.11	3.08	3.04	3.01	2.97	2.93	
9	5.12	4.26	3.86	3.63	3.48	3.37	3.29	3.23	3.18	3.14	3.07	3.01	2.94	2.89	2.86	2.83	2.79	2.75	2.71	
10	4.96	4.10	3.71	3.48	3.33	3.22	3.14	3.07	3.02	2.98	2.91	2.85	2.77	2.73	2.70	2.66	2.62	2.58	2.54	
11	4.84	3.98	3.59	3.36	3.20	3.09	3.01	2.95	2.90	2.85	2.79	2.72	2.65	2.60	2.57	2.53	2.49	2.45	2.40	
12	4.75	3.89	3.49	3.26	3.11	3.00	2.91	2.85	2.80	2.75	2.69	2.62	2.54	2.50	2.47	2.43	2.38	2.34	2.30	
13	4.67	3.81	3.41	3.18	3.03	2.92	2.83	2.77	2.71	2.67	2.60	2.53	2.46	2.41	2.38	2.34	2.30	2.25	2.21	
14	4.60	3.74	3.34	3.11	2.96	2.85	2.76	2.70	2.65	2.60	2.53	2.46	2.39	2.34	2.31	2.27	2.22	2.18	2.13	
15	4.54	3.68	3.29	3.06	2.90	2.79	2.71	2.64	2.59	2.54	2.48	2.40	2.33	2.28	2.25	2.20	2.16	2.11	2.07	
16	4.49	3.63	3.24	3.01	2.85	2.74	2.66	2.59	2.54	2.49	2.42	2.35	2.28	2.23	2.19	2.15	2.11	2.06	2.01	
17	4.45	3.59	3.20	2.96	2.81	2.70	2.61	2.55	2.49	2.45	2.38	2.31	2.23	2.18	2.15	2.10	2.06	2.01	1.96	
18	4.41	3.55	3.16	2.93	2.77	2.66	2.58	2.51	2.46	2.41	2.34	2.27	2.19	2.14	2.11	2.06	2.02	1.97	1.92	
19	4.38	3.52	3.13	2.90	2.74	2.63	2.54	2.48	2.42	2.38	2.31	2.23	2.16	2.11	2.07	2.03	1.98	1.93	1.88	
20	4.35	3.49	3.10	2.87	2.71	2.60	2.51	2.45	2.39	2.35	2.28	2.20	2.12	2.07	2.04	1.99	1.95	1.90	1.84	
21	4.32	3.47	3.07	2.84	2.68	2.57	2.49	2.42	2.37	2.32	2.25	2.18	2.10	2.04	2.01	1.96	1.92	1.87	1.81	
22	4.30	3.44	3.05	2.82	2.66	2.55	2.46	2.40	2.34	2.30	2.23	2.15	2.07	2.02	1.98	1.94	1.89	1.84	1.78	
23	4.28	3.42	3.03	2.80	2.64	2.53	2.44	2.37	2.32	2.27	2.20	2.13	2.05	2.00	1.96	1.91	1.86	1.81	1.76	
24	4.26	3.40	3.01	2.78	2.62	2.51	2.42	2.36	2.30	2.25	2.18	2.11	2.03	1.97	1.94	1.89	1.84	1.79	1.73	
25	4.24	3.39	2.99	2.76	2.60	2.49	2.40	2.34	2.28	2.24	2.16	2.09	2.01	1.95	1.92	1.87	1.82	1.77	1.71	
26	4.23	3.37	2.98	2.74	2.59	2.47	2.39	2.32	2.27	2.22	2.15	2.07	1.99	1.94	1.90	1.85	1.80	1.75	1.69	
27	4.21	3.35	2.96	2.73	2.57	2.46	2.37	2.31	2.25	2.20	2.13	2.06	1.97	1.92	1.88	1.84	1.79	1.73	1.67	
28	4.20	3.34	2.95	2.71	2.56	2.45	2.36	2.29	2.24	2.19	2.12	2.04	1.96	1.91	1.87	1.82	1.77	1.71	1.65	
29	4.18	3.33	2.93	2.70	2.55	2.43	2.35	2.28	2.22	2.18	2.10	2.03	1.94	1.90	1.85	1.81	1.75	1.70	1.64	
30	4.17	3.32	2.92	2.69	2.53	2.42	2.33	2.27	2.21	2.16	2.09	2.01	1.93	1.88	1.84	1.79	1.74	1.68	1.62	
40	4.08	3.23	2.84	2.61	2.45	2.34	2.25	2.18	2.12	2.08	2.00	1.92	1.84	1.78	1.74	1.69	1.64	1.58	1.51	
60	4.00	3.15	2.76	2.53	2.37	2.25	2.17	2.10	2.04	1.99	1.92	1.84	1.75	1.69	1.65	1.59	1.53	1.47	1.39	
120	3.92	3.07	2.68	2.45	2.29	2.17	2.09	2.02	1.96	1.91	1.83	1.75	1.66	1.60	1.55	1.50	1.43	1.35	1.25	
$\infty$	3.84	3.00	2.60	2.37	2.21	2.10	2.01	1.94	1.88	1.83	1.75	1.67	1.57	1.51	1.46	1.39	1.32	1.22	1.00	